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## ***Structural Design of Hydraulic Structures***

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# **Design of Prestress Members**

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## **Design of Prestress Members**

As in reinforced concrete problems, in prestressed concrete can be separated generally as analysis problems or design problems.

**Flexural design based on concrete stress limit:**

**OR (allowable stress design method):**

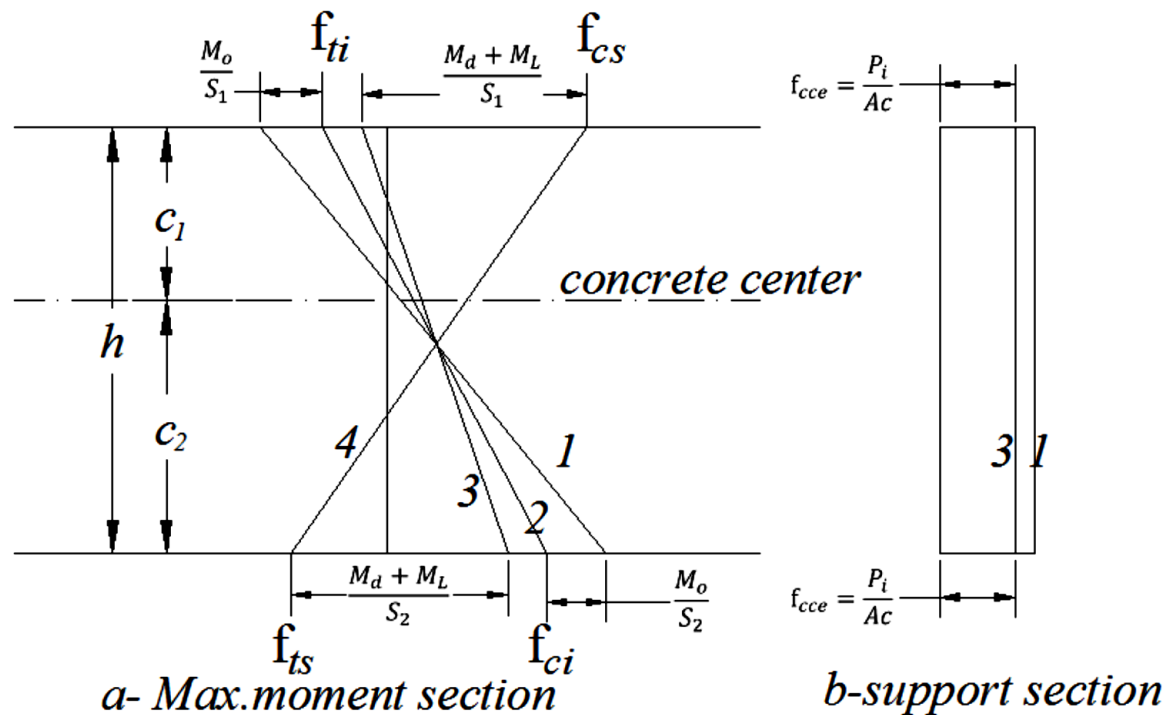
If the dimensions of a concrete section, the amount of prestress area  $A_{ps}$ , the prestress force  $P_i$  or  $P_e$  and eccentricity location  $e$  are to be found; the problems must be design according to the allowable stresses of ACI with many interrelated variables.

### **a- Beam with variable eccentricity:**

For a typical class U or T beam in which tendon eccentricity permitted to vary along span flexural stress distribution in the concrete at the maximum moment section are shown in Figure (4-1).

Summarizing the design process to determine the best cross section and the required prestress force and eccentricity based on stress limitations.

The requirement for the section moduli  $S_1$  and  $S_2$  with respect to the top and bottom surfaces respectively is:



1- $P_i$

2- $P_i + M_g$

3- $P_e + M_g$

4- $P_e + M_t$

**Figure (4-1) Flexural stress distribution for beam with variable eccentricity**  
**(a) maximum moment section (b) support section**

**b- Beam with constant eccentricity:**

The design method presented in the previous section was based on stress conditions at the maximum moment section of a beam with the maximum value of moment ( $M_g$ ). If  $P_i$  and  $e$  were to held constant along the span, the eccentricity is controlled by conditions at the supports,

where  $M_g = \text{Zero}$ . The requirements on the section moduli are that:

$$S_1 \geq \frac{(1-R) M_g + M_d + M_L}{R f_{ti} - f_{cs}}$$

$$S_2 \geq \frac{(1-R) M_g + M_d + M_L}{f_{ts} - R f_{ti}}$$

$$R = \text{effective ratio} = \frac{P_e}{P_i}$$

$$P_e = R \times P_i$$

$$R = 1 - \text{Losses}$$

$$S_1 = \frac{I_c}{C_1}, \quad S_2 = \frac{I_c}{C_2}$$

$$I_c = S_1 C_1 = S_2 C_2$$

$$\frac{C_1}{C_2} = \frac{S_2}{S_1}$$

Or in terms of total section depth:

$$h = C_1 + C_2$$

$$\frac{C_1}{h} = \frac{S_2}{S_1 + S_2}$$

The concrete centroid stress under initial condition  $f_{cci}$  is given:

$$f_{cci} = f_{ti} - \frac{C_1}{h} (f_{ti} - f_{ci})$$

The initial prestress force is:

$$P_i = A_c |f_{cci}|$$

$e_{max}$  at the maximum moment section:

$$e_{max} = e = (f_{ti} - f_{cci}) \frac{S_1}{P_i} + \frac{M_g}{P_i}$$

Or

The same result will be obtained from consideration of requirement at the bottom fiber.

$$e_{max} = e = (f_{cci} - f_{ci}) \frac{S_2}{P_i} + \frac{M_g}{P_i}$$

The required area of pre-stressing steel  $A_{Ps}$ :

$$A_{Ps} = P_i / \text{permissible stress in the steel}$$

Permissible stress in the strand immediately after transfer must not exceed  $0.82 f_{Py}$  or  $0.74 f_{Pu}$ .

The requirements on the section moduli are that:

$$S_1 \geq \frac{M_g + M_d + M_L}{R f_{ti} - f_{cs}}$$

$$S_2 \geq \frac{M_g + M_d + M_L}{f_{ts} - R f_{ci}}$$

The required eccentricity is:

$$e = (f_{ti} - f_{cci}) \frac{S_1}{P_i}$$

or

$$e = (f_{cci} - f_{ci}) \frac{S_2}{P_i}$$

The concrete centroid stress and the initial prestress force may be found as before in previous section.

## **Step of design procedure:**

**a-** Assume a concrete section

**b-** Calculate the required prestresses force and eccentricity.

For that will be the controlling load stage

**c-** Check the stresses at all stage

**d-** Check the flexural strength

The trial section is then evicted if necessary.