

Fluid Flow in Pipes

What you have to know before start?

- 1- Real Flow, this mean that the viscosity term work affectively ($\mu \neq 0$).
- 2- Ideal Flow, this mean that the viscosity term can be neglected ($\mu = 0$).
- 3- Reynold Number, this number can be used to test whether the flow is **Laminar or Turbulent**. Where,

$$\text{Laminar}, Re \leq 2100$$

$$\text{Transitional flow}, 2100 < Re < 4000$$

$$\text{Turbulent}, Re \geq 4000$$

All these limitations are for internal flow.

- 4- Reynold Number, dimensionless number:

$$Re = \frac{\rho * V * D}{\mu}$$

- 5- Total head loss can be calculated by using Darcy Weisbach Equation:

$$\Delta P = \frac{f \cdot L}{D} * \frac{V^2}{2}$$

OR in the Head Form

$$h_f = \frac{f \cdot L}{D} * \frac{V^2}{2g}$$

is very important for the engineering design and operation of pipe systems. It shows that the pressure drop of a fully-developed pipe flow is a function of three parameters, i.e., **the friction factor f , pipe geometry (L/D)**.

The friction factor f , it can be calculated for both cases by:

a- Laminar Flow:

$$f = \frac{64}{Re}$$

By substitute in the main equation will get:

$$h_f = \frac{32 \cdot \mu \cdot L \cdot V}{\rho \cdot g \cdot D^2}$$

b- Friction factor for turbulent flow:

for turbulent flow, it is impossible to analytically derive the friction factor f , which can ONLY be obtained from experimental data. In addition, most pipes, except glass tubing, have rough surfaces. The pipe surface roughness is quantified by a dimensionless number, relative pipe roughness (ε/D)

Where, ε is pipe roughness and D is pipe diameter.

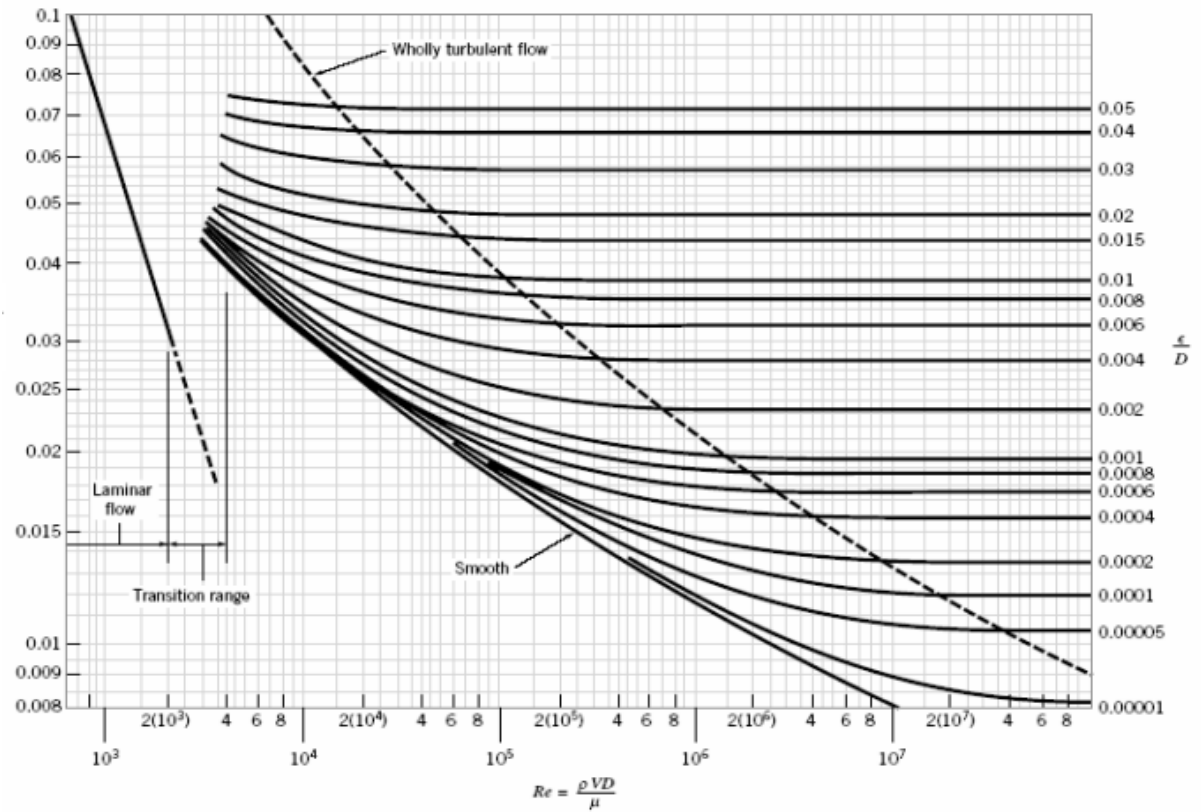
For smooth pipe:

$$f = \frac{0.316}{Re^{0.25}}$$

For roughness pipe:

The best way to find friction factor f , for rough pipe by using **Moody chart**.

To use the Moody chart, we need to calculate the relative roughness (ε/D) and Re for the flow under consideration. Hence, use the chart with the calculated values to find the friction factor.



Example 1: At 30 °C, glycerine (viscosity $\mu = 0.4 \text{ N}\cdot\text{s}/\text{m}^2$, density $\rho = 1,260 \text{ kg}/\text{m}^3$) flows at a rate of 180 mL/min through a horizontal 25 mm diameter smooth steel pipe.

- Determine the Reynolds number of the flow;
- Calculate the pressure gradient in Pa/m.

Solution:

$$\text{a- } Q = 180 \frac{\text{mL}}{\text{min}} = 0.18 \frac{\text{L}}{\text{min}} = 3 \times 10^{-6} \text{ m}^3/\text{sec}$$

$$\text{velocity} = \frac{\text{discharge}}{\text{Area}} = \frac{3 \times 10^{-6}}{\frac{\pi}{4} * 0.025^2} = 0.0061 \text{ m/sec}$$

Now, Reynolds number can be calculated by:

$$Re = \frac{\rho * u * d}{\mu} = \frac{1260 * 0.0061 * 0.025}{0.4} = 0.48$$

Base on the Reynolds number, the flow is laminar cause it is less than 2300.

- The pressure gradient can be calculated:

$$\frac{\Delta p}{L} = f * \frac{1}{D} * \frac{\rho * u^2}{2}$$

The friction factor can be calculated for laminar flow by:

$$f = \frac{64}{Re} = \frac{64}{0.48} = 133.3$$

$$\frac{\Delta p}{L} = 133.3 * \frac{1}{0.025} * \frac{1260 * 0.0061^2}{2} = 125 \text{ pa/m}$$

Example 2: At 20 °C, glycerine (viscosity $\mu = 0.62 \text{ N}\cdot\text{s}/\text{m}^2$, density $\rho = 1,260 \text{ kg}/\text{m}^3$) flows in a 25 mm diameter steel pipe at an average velocity of 0.3 m/s.

- Determine whether the flow is laminar or turbulent;
- Calculate the shear stress at the centre of the pipe and at the wall;
- If the pipe is vertical and the flow downward, what is the rate of change of pressure along the pipe?

Solution:

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$$Re = \frac{\rho * u * d}{\mu} = \frac{1260 * 0.3 * 0.025}{0.62} = 15.24$$

Base on the Reynolds number, the flow is laminar cause it is less than 2300.

b- Shear stress can be calculated by:

$$\Delta p = \frac{\tau_w * 4L}{d}$$

And we have the pressure drop as below:

$$\Delta p = f * \frac{L}{D} * \frac{\rho * u^2}{2} = \frac{\tau_w * 4L}{d}$$

$$\tau_w = \frac{f * \rho * u^2}{8}$$

The friction factor can be calculated for laminar:

$$f = \frac{64}{Re} = \frac{64}{15.24} = 4.2$$

$$\tau_w = \frac{4.2 * 1260 * 0.3^2}{8} = 59.53 \frac{N}{m^2}$$

c-

$$\frac{\Delta p}{L} = f * \frac{1}{D} * \frac{\rho * u^2}{2} = 4.2 * \frac{1}{0.025} * \frac{1260 * 0.3^2}{2} = 9524 \frac{pa}{m}$$

Test Yourself

- 1- Oil ($\rho = 800 \text{ kg/m}^3$) flow through a 50mm-diameter smooth pipe at a velocity of 2m/s, the pressure drops due to friction loss in the pipe 5023 pa. The pipe length is 10m.
 - a- Calculate the friction factor, f .
 - b- Determine whether the flow is laminar or turbulent.
 - c- Calculate the oil viscosity.
- 2- A steel pipe ($\epsilon = 0.045\text{mm}$), 500 mm in diameter and 5 km long carries 100,000 m³. water (viscosity $\mu = 1.15 \times 10^{-3} \text{ N}\cdot\text{s/m}^2$, density $\rho = 1,000 \text{ kg/m}^3$) per day. (a) Determine the pressure drop in the line; (b) Determine the pressure drop in a same-size concrete ($\epsilon = 0.91\text{mm}$) pipe; (c). If the concrete pipe is of a rectangular shape (length = 800 mm, width = 400 mm), what is the pressure drop in the line?

(b) 0.0157 (d) $487 \times 10^{-6} \text{ N}\cdot\text{s/m}^2$]

[Ans. (a) 2.19 MPa (b) 3.97 MPa (c) 2.84 MPa]

- 3- A capillary tube is 30 mm long and 1 mm bore. The head required to produce a flow rate of 8 mm³/s is 30 mm. The fluid density is 800 kg/m³. Calculate the dynamic and kinematic viscosity of the oil.

$$\mu = 0.0241 \text{ N s/m}$$

- 4- Water at 15 C° flows through a 25 cm diameter riveted steel pipe of length 450 m and roughness $\epsilon = 3.2$ mm. The head loss is known to be 7.30 m. Find the volumetric flow rate of water in the pipe.

$$U = 1.39 \text{ m/s}$$